



SKILL 5: Prime Factorization with Exponents

You can use exponents to express prime factorization in a compact form. For example, 125 is equal to $5 \times 5 \times 5$ or 5^3 .

To write the prime factorization of 360 in exponential form, first write the factors in expanded form.

$$360 = 2 \times 2 \times 2 \times 3 \times 3 \times 5$$

Use exponents to show the number of identical factors.

$$\begin{array}{c}
 \text{two factors of } 3 = 3^2 \\
 \downarrow \qquad \qquad \qquad \downarrow \\
 2 \times 2 \times 2 \times 3 \times 3 \times 5 = 2^3 \times 3^2 \times 5 \\
 \uparrow \qquad \qquad \qquad \uparrow \qquad \qquad \qquad \uparrow \\
 \text{three factors of } 2 = 2^3 \qquad \qquad \qquad 5 = 5^1, \text{ but you} \\
 \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \text{need not write} \\
 \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \text{the exponent.}
 \end{array}$$

So, the exponential form of the prime factorization of 360 is $2^3 \times 3^2 \times 5$.

Example

Write the prime factorization $3^3 \times 5^2$ in standard form.

First write in expanded form. $3^3 \times 5^2 = \underbrace{3 \times 3 \times 3}_{27} \times \underbrace{5 \times 5}_{25} = 675$

Then multiply.

The standard form of the number $3^3 \times 5^2$ is 675.

Guided Practice

1. Write $2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 5$ using exponents.

$$2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 5 = 2^{\square} \times 3^{\square} \times 5^{\square}$$

2. Write the prime factorization $2^3 \times 7^2$ in standard form.

a. Write 2^3 in expanded form. _____

b. Multiply the factors in part a. _____

c. Write 7^2 in expanded form. _____

d. Multiply the factors in part c. _____

e. Multiply the numbers you found in parts b and d. _____

f. So, $2^3 \times 7^2 = 2 \times \underline{\quad} \times \underline{\quad} \times 7 \times \underline{\quad} = 8 \times \underline{\quad} = \underline{\quad}$.

SKILL 5: Practice

Write the prime factorization for each number in expanded form as a product of individual factors. Then write each prime factorization using exponents.

1. 144

2. 90

3. 1,925

4. 480

5. 405

6. 444

7. 128

8. 225

9. 2,600

Write each prime factorization in expanded form. Then write the number in standard form.

10. $2^3 \times 3 \times 5^3$

11. $2^2 \times 3^3 \times 7^2 \times 11$

12. Luis used exponents to write this prime factorization for a number: $2^3 \times 3^3 \times 5^3$
What is the standard form for this number? _____



13. Which is the prime factorization for 720 using exponents?

Skill 5

A $2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5$

B $2^4 \times 3^2 \times 5$

C $2^3 \times 3^2 \times 5$

D $2 + 2 + 2 + 2 + 3 + 3 + 5$

14. Which is 7^3 in standard form?

Skill 4

F 21

G 37

H 73

J 343