Thinking With Mathematical Models Answers





Skill: Identifying Inverse Variation

- **1.** Inverse variation; xy = 70
- **2.** Inverse variation; xy = 48
- **3.** Direct variation; y = 11x
- **4.** Direct variation; y = 4.5x
- **5.** Inverse variation; xy = 36
- **6.** Inverse variation; xy = 6

Investigation 4 Additional Practice

- **1. a.** As circumference of a tree increases, so does its age in years.
 - **b.** Sample answer: Around 38 years, because 38 is between 34 and 43, the ages of the trees in the table with circumferences of 45 and 57 inches respectively.



- **b.** $y = \frac{15}{23}c + \frac{160}{23}$
- c. Actual: approximately 0.99; Sample answer: All points lie very close to the line, and the correlation is positive, so a value near 1.0 is to be expected.
- **3. a.** Sample answers: A: 0.98; B: -0.85; C: 0.15; D: -0.8 **b.** C, D, B, A
- 4. a. The number of hours of sleep needed to feel rested decreases as age increases.
 - **b.** -0.5; There is a negative correlation because the slope of the line is negative. The data values appear linear but are not very close to the line, so the correlation is not very strong.
 - c. Sample answer: No; the trend is probably not valid for higher ages, because if the trend continues, at a certain age people would no longer need to sleep at all.



b. Group A has a greater spread of scores, with a center around 50 words remembered.

Group B has a smaller spread of scores, with a center around 70 words remembered.

6. a. Group A mean: 51; median: 50; standard deviation: approx. 5.27 Group B mean: 70; median: 71; standard deviation: approx. 7.94 **b.** No; the study was for people who studied by reading silently or using art techniques. Neither of these categories includes using a computer game.



- **b.** The outside temperature appears to have some effect on the number of swimmers, but it has little effect on the number of registrants for free gym. There appears to be a linear association in the swimming pool data, but not in the free gym data.
- **c.** No; the data for free gym weakens the correlation, so it would be better to use a model line that represents only the swimming pool data points.
- **8. a.** The number of people who attend the swimming pool is fairly spread out with a center around 37.
 - **b.** The number of people who attend free gym in clustered around 37.5.
- **9.** The data are positively correlated. The correlation coefficient is closest to 0.50.
- **10.** D, B, C, A
- **11. a.** mean
 - **b.** median
 - **c.** standard deviation

Skill: Describing Data Sets

- **1.** The total boat rental charge increases at a rate of \$15 per hour.
- **2.** The snow is falling at a rate of 1.25 inches per hour.

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- **3.** The drink price increases at a rate of \$0.07 per ounce.
- **4.** The plant has been growing at a rate of 0.25 inch per week.
- **5.** The pool is draining at a rate of 1.6 gallons per minute.
- 6. The ice cube height is decreasing at a rate of 0.64 centimeter per minute as it melts.
- 7. The outside temperature is decreasing 12°F per hour or 0.2°F per minute.
- **8.** The games cost an average of \$3 each.
- 9. Mean: 18; median 12; st. dev.: approx. 18.97
- 10. Mean: 1.2; median 1.2; st. dev.: approx. 0.17
- **11.** Mean: 132; median 136; st. dev.: approx. 10.49
- **12.** Mean: 6.7; median: 6.95; st. dev.: approx. 1.67
- **13.** Mean: 3.5; median: 3.5; st. dev.: approx. 0.59
- 14. Mean: 70; median: 70.5; st. dev.: approx. 4.15
- **15.** Mean: 140; median: 140; st. dev.: 30
- **16.** Mean: $89.\overline{4}$; median: 90; st. dev.: approx. 7.14

Investigation 5 Additional Practice

- 1. Examples will vary.
 - a. categorical g. categorical
 - **b.** numerical **h.** numerical
 - **c.** numerical i. categorical
 - **d.** either j. categorical
 - **e.** numerical **k.** categorical
 - **f.** categorical I. either
- 2. Sample answers: numerical: time length, speed, number of measures, number of parts, prices; categorical: genre, instrumentation, format
- **3. a. Sample answer:** false, because 24% of seventh graders prefer pop music compared to 24.4% of eighth graders.
 - **b.** Sample answer: true, because equal numbers of people who like country music are in sixth or seventh grade.
 - c. Sample answer: true, because fewer eighth graders prefer pop music than rock music.
 - d. Sample answer: false, because 20% of sixth graders prefer rock music while 17.4% of eighth graders prefer other types of music.

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4.	а.	

-		C	Р	R	0
	6th	25%	30%	20%	25%
	7th	20%	24%	24%	32%
	8th	33%	24%	26%	17%

b.		С	Р	R	0
	6th	29%	34%	25%	29%
	7th	29%	34%	38%	47%
	8th	43%	31%	38%	24%

С.		С	Р	R	0	Т
	6th	7%	9%	6%	7%	29%
	7th	7%	9%	9%	12%	37%
	8th	11%	8%	9%	6%	34%
	т	25%	26%	24%	25%	100%



5.

a.		Music	Games	Total	
	< 18	62	64	126	
	18-29	54	59	113	
	30-50	45	51	96	
	> 50	15	10	25	
	Total	176	184	360	

b.		Music	Games	Total	
	< 30	116	123	239	
	≥ 30	60	61	121	
	Total	176	184	360	

- c. Sample answer: No, because 116 is less than twice 60.
- **d.** Sample answer: It is more likely that they will purchase games, because 123 > 116.
- e. Sample answer: It is about equally likely that a person over 30 will purchase music or games, because both percents are close to 50%.

6. a.

Direct Sun	Coverage in Blooms				
	< Avg. Avg. > Avg.				
Partial	40%	50%	10%		
Full	15%	25%	60%		



- **c.** Sample answer: No, because only 60% of the bushes planted in partial sunlight produced at least an average number of blooms compared to 85% of bushes planted in full sunlight.
- 7. 60%
 - 24 out of 40

8.
$$\frac{6}{60} = \frac{1}{10} = 10\%$$

9. (Figure 1)

Skill: Proportions and Percents

- **1.** $\frac{3}{30}, \frac{10}{100}, \frac{15}{150}$
- **2.** $\frac{7.5}{30}, \frac{25}{100}, \frac{37.5}{150}$
- **3.** $\frac{10}{30}$, approximately $\frac{33.3}{100}$, $\frac{50}{150}$
- **4.** $\frac{12}{30}, \frac{40}{100}, \frac{60}{150}$
- **5.** $\frac{15.6}{30}, \frac{52}{100}, \frac{78}{150}$
- $\frac{19.5}{30}, \frac{65}{100}, \frac{97.5}{150}$ 6.
- <u>21.3</u> <u>71</u> <u>1</u>06.5 7. $\overline{30}$, $\overline{100}$, $\overline{150}$
- **8.** $\frac{24.15}{30}, \frac{80.5}{100}, \frac{120.75}{150}$

Figure 1

	Blue	Red	Green	Orange
7th grade	20%	28%	40%	12%
8th grade	16%	44%	32%	8%

- <u>29.7</u> <u>99</u> 148.5 9. 30, 100, 150 33 110 165 10. $\overline{30}, \overline{100}, \overline{150}$ 45 150 225 11. $\overline{30}$, $\overline{100}$, $\overline{150}$ 60 200 300 12. $\overline{30}, \overline{100}, \overline{150}$ **13.** 20 **14.** 33.3% **15.** 93.8% **16.** 66% **17.** 30% **18.** 36.0%
- **19.** 166.7%
- **20.** 117.6%
- 21. 206.3%